REVISED: Report # 3237

To: Faculty Council

From: Professor Greg A. Jamieson  
Chair, Curriculum Committee

Date: November 19, 2009

Item: Supplement to Proposed Curriculum Updates for 2010/2011 Faculty Calendar - Proposed Engineering Science Major in Engineering Mathematics and Finance

The Curriculum Committee presents herewith a supplement to its proposed updates to Chapters 7 and 8 of the 2010/2011 Faculty Calendar.
1. Proposed Engineering Science Option/Major\(^1\) in Engineering Mathematics and Finance

**Engineering Mathematics and Finance Major Proposal**

**October 2009**

**Introduction:**

In April 2008, a working group was struck to examine the idea of developing a Major in Engineering Science in the field of Financial Engineering. This idea grew out of a grassroots interest in hosting such a Major from the Department of Mechanical and Industrial Engineering (MIE) and was encouraged by the Division of Engineering Science when the decision was made by MIE to cancel the Manufacturing Systems Option.

The working group has the following membership:

- Professor Roy Kwon (MIE)
- Professor Daniel Frances (MIE)
- Professor Yuri Lawryshyn (Chemical Eng. & Applied Chemistry)
- Professor Sebastian Jaimungal (Statistics)
- Professor Alan White (Rotman)
- Mr. Glynn Williams (alumnus)
- Dr. Murray Metcalfe (alumnus)
- Ms. Angela Tran (graduate student)
- Ms. Lisa Romkey (EngSci)
- Professor Will Cluett (EngSci)

A proposal for a Major in this field, with the proposed name “Engineering Mathematics and Finance”, is outlined in this document. The choice of name, Engineering Mathematics and Finance, was made because it is an engineering program built around advanced courses in mathematics and statistics with finance as an integral part of the program. A minor change to the name may be made to reflect the contributions to the proposed curriculum from both mathematics and statistics. Should this name change occur, it will be provided to Faculty Council for information in February 2010.

The working group feels that this would be an excellent fit for Engineering Science because (1) this is a critical area of importance in the modern world where having a quantitative/engineering background is a great advantage, (2) many Engineering Science students have expressed interested in such a Major, and (3) the background required for successful participation in the field is exactly the type of background that Engineering Science provides.

This area is highly relevant to Engineering Science because it is engineering in the most modern yet traditional sense. By now there is a wide body of financial theory in place to explain the dynamics of financial instruments and markets that impact just about

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\(^1\) As approved by the Academic Policy and Programs Committee (Item of April 24, 2008), Options in Engineering Science are now referred to as Majors on student transcripts. However, the word Option continues to be used to refer to the various choices Engineering Science students have available to them prior to entering Year 3 and 4.
everyone in the world. This characterization is highly rigorous, mathematical, quantitative, and statistical, not unlike mathematical descriptions of the physical phenomena that underpin the more traditional Engineering Science Majors.

The essence of design in this field is based on practical constructs just like the design of a bridge would be for civil engineers except that the underpinning is mathematical financial theory. The designs in this field are more abstract than a bridge design but every bit as practical e.g. a firm can engage in a contract design that minimizes risks, or the design of a portfolio of stocks to ensure a high quality of living for people participating in pension plans. The promise of the field is in the design of better financial arrangements for society.

A number of leading engineering schools around the world have already recognized that Financial Engineering fits within engineering (see below for examples at Princeton, Columbia, Stanford). U of T is a leading institution world-wide and the Engineering Science program is one of the most analytically demanding undergraduate programs at the University. Therefore, these students are well matched for the demanding rigor of Financial Engineering and will be well prepared to enter both the financial industry as well as tier 1 North American graduate school programs in related fields.

Princeton: 
http://orfe.princeton.edu/

Columbia: 

Stanford: 
http://www.stanford.edu/dept/MSandE/
Learning Outcomes:
The Engineering Science Major in Engineering Mathematics and Finance aligns with the Engineering Science program's degree level expectations. In particular, the Major will result in graduates that have:

- An understanding of financial market/instruments in terms of their role in society at large (capital markets, financial institutions, corporate finance)
- An understanding of the mathematical/computational/computing aspects of modern markets/instruments (stochastic calculus, optimization theory, statistics and financial econometrics, trading systems, programming, numerical computation)
- Explored some of the important problems in modern finance, including (a) pricing of contracts and (b) construction of financial portfolios
- Tackled financial engineering problems as they may occur in whatever possible variety
- Developed a quantitative background that would be sufficient preparation for graduate school in finance, operations research, applied mathematics, etc.

Recommended Themes:

Theme #1: Math/Stats
- Real Analysis
- Probability
- Stochastic Processes
- Time Series, Statistical Computation & Financial Econometrics

Theme #2: Finance/Financial Engineering
- Omnibus course in micro, macro, corporate finance and accounting
- Option Pricing
- Portfolio Optimization
- Financial Engineering
- Real Options

Theme #3: Computation
- PDE’s and Numerical Methods
- Optimization
- Monte Carlos Methods
- Time Series & Statistical Computation
## Proposed Curriculum:

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<tbody>
<tr>
<td>• Engineering Economic Analysis &amp; Decision Making (CHE374)</td>
<td>• Engineering Finance and Economics (CHE3XX)(^5)</td>
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<tr>
<td>• Probability (STA347)</td>
<td>• Intro to Real Analysis (MAT337) OR Real Analysis I (MAT357)</td>
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<td>• Financial Engineering (MIE375)(^2)</td>
<td>• Financial Principles for Actuarial Science (ACT370)</td>
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<td>• Partial Differential Equations (APM384)(^3)</td>
<td>• Financial Optimization Models (MIE377)(^6)</td>
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<td>• Mathematical Programming (Optimization) (MIE376)(^4)</td>
<td>• Methods of Data Analysis (STA302)</td>
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<td>• Option Seminar (ESC301)</td>
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<td>• Thesis</td>
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<td>• HSS/CS elective</td>
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<td>• Stochastic Methods (ACT460)</td>
<td>• Capstone Design (MIE479)(^7)</td>
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<td>• EM&amp;F Elective #1</td>
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<td>• EM&amp;F Elective #2</td>
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\(^2\) New course being proposed by MIE.
\(^3\) Course should be modified to include numerical methods.
\(^4\) New course being proposed by MIE.
\(^5\) New course being proposed by MIE.
\(^6\) New course being proposed by MIE.
\(^7\) New course being proposed by MIE.
New Course Descriptions:

MIE375: Financial Engineering

This course provides a background in the fundamental areas in financial engineering including relevant concepts from financial economics. Major topics include interest rate theory, fixed income securities, bond portfolio construction, term structure of interest rates, mean-variance optimization theory, the Capital Asset Pricing Model (CAPM), arbitrage pricing theory (APT), forwards and futures, and introduction to option pricing and structured finance.

MIE376: Mathematical Programming

This course deals with the formulation of optimization models for the design and operation of systems that produce goods and services, and the solution of such problems with mathematical programming methods, including linear programming: the simplex method, sensitivity analysis, duality, the revised simplex, column generation, Dantzig-Wolfe decomposition and linear programming with recourse; minimum cost network flows; dynamic programming; integer programming; non-linear programming models.

MIE377: Financial Optimization Models

This course deals with the formulation of optimization models for the design and selection of an optimal investment portfolio. Topics include Risk Management, Mean Variance Analysis, Models for Fixed Income, Scenario Optimization, Dynamic Portfolio Optimization with Stochastic Programming, Index Funds, Designing Financial Products, and Scenario Generation. These concepts are also applied to International Asset Allocation, Corporate Bond Portfolios and Insurance Policies with Guarantees.

CHE375: Engineering Finance and Economics

This course consists of three modules: 1) managerial accounting, 2) corporate finance and 3) macro economics. The first module, managerial accounting, will consist of an introduction to financial statements and double entry recordkeeping, then delve deeper into aspects of revenue, expenses, assets, debt and equity. The second module, corporate finance, will introduce the concept of risk and return, and the Capital Asset Pricing Model, and then delve deeper into capital budgeting, corporate financing, financial statement analysis and financial valuation. The third model, macro economics, will introduce global aspects of business, including economic, political, societal and technological, then discuss factors such as GDP, inflation, unemployment, interest rates, foreign exchange rates, fiscal debt/surplus and balance of payments, and their impact on the financials of a given country.
Ideas for a Capstone Design Course MIE479: Engineering Mathematics and Finance Capstone Design

The course would involve group projects where, given the field, the team would build a tool, likely a computer based mathematical modeling system.

1. The project should solve a real problem, and not be a theoretical derivation. Testing in the real world, perhaps with industry involvement, would be helpful in that regard. In particular the team might be required to explain to those who are not financial engineers themselves the purpose of the project and the approach as it evolves, to keep it tied to real world.

2. The project should be in a domain that is clearly technology/engineering related and driven. This way the project will tie to the broader engineering discipline.

3. To pull this into the real world further, there might there be a component of the modeling system that is real time, perhaps deriving data from some type of sensors or signaling mechanism.

4. The capstone project model might involve optimizing against an objective (i.e. goal) function that includes factors other than economic/monetary. This will likely make the project quite different from most of the Major course work and will be a "mind expander" for the students. It might include environmental and social factors - so called triple bottom line analysis - that would need to be factored in. There could already be work done in this field in the case of carbon markets and carbon credits. This type of multi-variable approach could become a specific research theme that faculty members might get involved in.
Engineering Mathematics and Finance Major: Fourth-Year Electives

In Year 4 of the proposed curriculum, students select 4-5 EM&F electives, depending on whether they do a half-year or full-year thesis, from the list of courses below. Students are required to take at least two from Group A and at least two from one of the domains in Group B. In addition, students must select their electives such that they meet accreditation requirements. These courses are subject to change and will be finalized for the 2011-2012 Faculty Calendar, the year in which the 4th Year of this Major will be first offered.

Group A: Methodologies and Tools Courses

- APM466 Mathematical Theory of Finance
- CHE507 Data-based Modelling for Prediction and Control
- ECE358 Foundations of Computing
- ECO462 Financial Econometrics
- MIE360 Systems Modelling and Simulation
- MIE365 Operations Research II
- MIE367 Cases in Operations Research
- MIE457 Knowledge Modelling and Management
- MIE562 Scheduling
- MIE566 Decision Analysis
- RSM430 Fixed Income Securities
- RSM432 Risk Management for Financial Managers
- STA410 Statistical Computation
- STA447 Stochastic Processes
Group B: Domain Courses

Aerospace
AER302  Aircraft Flight
AER315  Combustion Processes

Biomedical
BME340  Biomedical Engineering Instrumentation and Technology
BME350  Physiological Control Systems
BME395  Cellular and Molecular Bioengineering I

Electrical and Computer
ECE349  Introduction to Energy Systems
ECE352  Computer Organization
ECE353  Systems Software
ECE360  Electronics

Energy & the Environment
APS510  Technologies and Organizations in Global Energy Systems
CHE308  Chemical Processes for Energy Generation and Storage
CIV300  Terrestrial Energy Systems
CIV301  Design of Hydro and Wind Electric Plants
CIV440  Environmental Impact and Risk Assessment
ECE359  Energy Conversion
MIE303  Mechanical and Thermal Energy Conversion Processes
MIE315  Design for the Environment
MIE515  Alternative Energy Systems

Infrastructure
CIV352  Structural Design I
CIV357  Structural Design II
CIV359  Intelligent Transportation Systems
CIV460  Engineering Project Finance and Management
CIV516  Public Transit Operations and Planning
CIV531  Transport Planning

Manufacturing
AER525  Robotics
CHE561  Risk Based Safety Management
MIE221  Manufacturing Engineering
MIE422  Automated Manufacturing
MIE440  Mechanical Design: Theory and Methodology
MIE469  Reliability and Maintainability Engineering
MIE540  Product Design

Mining
CME321  Geotechnical Engineering I
MIN401  Mineral Reserve and Mineral Resource Estimation
MIN430  Mining Environmental Management
Course Descriptions for technical electives from outside the Faculty:

**STA410 Statistical Computation**


**STA447 Stochastic Processes**

Discrete and continuous time processes with an emphasis on Markov, Gaussian and renewal processes. Martingales and further limit theorems. A variety of applications taken from some of the following areas are discussed in the context of stochastic modeling: Information Theory, Quantum Mechanics, Statistical Analyses of Stochastic Processes, Population Growth Models, Reliability, Queuing Models, Stochastic Calculus, Simulation (Monte Carlo Methods).

**ECO462 Financial Econometrics**

This course is intended primarily for students in the Financial Economics specialist program. An introduction to the econometrics used in empirical finance, with an emphasis on estimation and inference using computer based applications. Topics will include parametric and nonparametric models of volatility, evaluation of asset pricing theories and models for risk management and transactions data.

**RSM430 Fixed Income Securities**

Describes important fixed income securities and markets. The course emphasizes traditional bond and term structure concepts crucial to understand the securities traded in these markets. Students are required to work in the Rotman Financial Research & Trading Lab to solve the assigned problems using real time data.

**RSM432 Risk Management for Financial Managers**

This course examines the ways in which risks are quantified and managed by financial institutions. The principal risks considered include market risk, credit risk and operational risk. The course also covers the evolution of bank regulation and the regulatory limits on risk taking.